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Mark Scheme (Results)
January 2012

International GCSE Mathematics
(4MA0) Paper 4H


#### Abstract

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January 2012
Publications Code UG030750
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Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

| Question | Working | Answer | Mark | Notes |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
| $\mathbf{1 .}$ | $\frac{4.2}{1.12}$ |  | 2 | M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$ |
|  |  | 3.75 |  | A1 |
|  |  |  |  |  |


| 2. | $\frac{135}{180}$ |  | 3 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | 0.75 oe |  |  | A1 |
|  |  | 45 |  | A1 cao |
|  |  |  |  | Total 3 marks |



| 6. (a) | $1+7$ or 8 |  | 2 | M1 | 8 may be denominator of fraction or coefficient in an equation such as $8 x=32$ | SC <br> If M0 A0, <br> award B1 <br> for 4 : 28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 28 |  | A1 | cao |  |
| (b) | $32 \times 45$ or 1440 or $14.4(0) \mathrm{m}$ |  | 3 | M1 |  |  |
|  | $\frac{" 1440 "}{72}$ |  |  | M1 | dep |  |
|  |  | 20 |  | A1 | cao |  |
|  |  |  |  |  |  | al 5 marks |


| 7. | Fully correct factor tree or repeated division <br> or $2,2,2,5,5$ or $2 \times 2 \times 2 \times 5 \times 5$ | 3 | M2M1 for factor tree or repeated <br> division with 2 and 5 as factors |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  | $2^{3} \times 5^{2}$ |  | A1 ${\text { Also accept } 2^{3} \cdot 5^{2}}^{\text {Total 3 marks }}$ |
|  |  |  |  |  |


| 8. | $y^{3+n-1}=y^{6}$ oe or $y^{3+n}=y^{7}$ oe <br> or $3+n-1=6$ oe <br> or $y^{n}=\frac{y^{7}}{y^{3}}$ or $y^{n}=\frac{y^{6}}{y^{2}}$ or $y^{n}=y^{4}$ | 2 | M1 | SC if M0, award B1 for <br> an answer of $y^{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 4 |  | A1 cao |


| 9. (a) | Complete, correct expression which, if correctly evaluated, gives 48 eg $4 \times \frac{1}{2} \times 6 \times 4,2 \times \frac{1}{2} \times 12 \times 4, \frac{1}{2} \times 12 \times 8$ |  | 3 | M2 M1 for correct expression for area of one relevant triangle$\begin{aligned} & \text { eg } \frac{1}{2} \times 6 \times 4, \frac{1}{2} \times 6 \times 4 \sin 90^{\circ} \\ & \frac{1}{2} \times 8 \times 6, \quad \frac{1}{2} \times 12 \times 4 \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 48 |  | A | cao |
| (b) | $4^{2}+6^{2}=16+36=52$ |  | 3 |  | for squaring and adding |
|  | $\sqrt{4^{2}+6^{2}}$ |  |  |  | (dep) for square root |
|  |  | 7.21 |  |  | for answer which rounds to 7.21 (7.211102...) |
|  |  |  |  |  | Total 6 marks |


| 10. (i) |  | $-1 \frac{1}{2}<x \leq 2$ | 4 |  | Also accept $-\frac{3}{2}<x \leq 2$ or answer expressed as two separate inequalities <br> B1 for $-1 \frac{1}{2}<x$ or $-\frac{3}{2}<x$ <br> or $x \leq 2$ (these may be as part of a double-ended inequality) <br> or $-\frac{6}{4}<x \leq \frac{8}{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (ii) |  | $\begin{array}{lllll}-1 & 0 & 1 & 2\end{array}$ |  |  | B1 for 4 correct and 1 wrong or for 3 correct and 0 wrong |
|  |  |  |  |  | Total 4 marks |


| 11. (a) | $\begin{aligned} & 75=3 \times 5^{2} \text { and } 90=2 \times 3^{2} \times 5 \\ & \text { or } 1,3,5,15,25,75 \text { and } \\ & 1,2,3,5,6,9,10,15,18,30,45,90 \\ & \text { or } 3 \times 5 \end{aligned}$ |  | 2 | M1 | Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 <br> Prime factors may be shown as factor trees or repeated division |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 15 |  | A1 |  |  |
| (b) | $2 \times 3^{2} \times 5^{2}$ oe eg $6 \times 3 \times 5^{2}$ or $75,150,225,300,375,450$ and $90,180,270,360,450$ |  | 2 |  | Also award for $\frac{75 \times 90}{15}$ |  |
|  |  | 450 |  | A1 |  |  |
|  |  |  |  | Total 4 marks |  |  |
|  |  |  |  |  |  |  |
| 12. (a) |  | Rotation | 3 | B1 |  | These marks are independent but award no marks if the answer is not a single transformation |
|  |  | $90^{\circ}$ |  | B1 | Also accept These <br> quarter turn or indepe <br> $-270^{\circ}$ <br> (B0 for $90^{\circ}$ award <br> clockwise) a sing  |  |
|  |  | $(0,0)$ |  | B1 | Also accept <br> origin, $O$ transf <br>   |  |
| (b) |  | R correct | 1 | B1 |  |  |
| (c) |  | Rotation $90^{\circ}$ | 2 | B1 | Accept quarter turn or $-270^{\circ}$ instead of $90^{\circ}$ | As for (a) |
|  |  | $(3,1)$ |  |  | ft from their $\mathbf{R}$ if it is a translation of the correct $\mathbf{R}$ |  |
|  |  |  |  | Total 6 marks |  |  |


| 13. (a) | $4 y=10-3 x$ or $-4 y=3 x-10$ |  | 3 |  | May be implied by second M1 or by $y=-\frac{3}{4} x+c$ even if value of $c$ is incorrect. or finds coordinates of 2 points on the line eg $(0,2.5), x=2, y=1$, table, diagram. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $y=\frac{5}{2}-\frac{3}{4} x$ oe or $y=\frac{10}{4}-\frac{3}{4} x$ oe or $y=\frac{10-3 x}{4}$ oe |  |  |  | or for clear attempt to evaluate $\frac{\text { vert diff }}{\text { horiz diff }}$ for their pts |
|  |  | $-\frac{3}{4}$ |  | A1 | Award 3 marks for correct answer if either first M1scored or no working shown. <br> $S C$ If M0, award B1 for $-\frac{3}{4} x$ |



| 14. (a) |  | $\begin{array}{lllllllllll}55 & 1155177190200\end{array}$ | 1 | B1 | cao |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  | Points correct | 2 | B1 | $\pm 1 / 2 \mathrm{sq} \mathrm{ft}$ from sensible table ie clear attempt to add frequencies |
|  |  | Curve or line segments |  | B1 | ft from points if 4 or 5 correct or ft correctly from sensible table or if points are plotted consistently within each interval at the correct heights <br> Accept curve which is not joined to the origin |
| (c) | 26 indicated on cf graph |  | 2 | M1 | for 26 indicated on cf graph - accept 26-27 inc |
|  |  | approx 60 from correct graph |  | 1 | If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve \& if answer is correct ( $\pm 1 / 2$ sq tolerance) award M1 A1 |
|  |  |  |  | Total 5 marks |  |
|  |  |  |  |  |  |
| 15. |  | $-4<x<4$ | 2 | B2 B1 for $x<4$ or $x>-4$ or $x< \pm 4$ or $x<\sqrt{16}$ <br> $S C$ B1 for $-4 \leq x \leq 4$ |  |
|  |  |  |  |  | Total 2 marks |


| 16. <br> (a) | $\frac{3}{8}+\frac{2}{8}$ oe |  | 2 | M1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\frac{5}{8}$ |  | A1 |  |  |
| (b)(i) | $\frac{2}{8} \times \frac{1}{7}$ appearing once only |  | 5 | M1 |  | Sample space method award 2 marks for correct answer; otherwise no marks |
|  |  | $\frac{2}{56}$ or $\frac{1}{28}$ |  | A1 | for $\frac{2}{56}$ or $\frac{1}{28}$ <br> or for 0.036 <br> or for answer rounding to 0.036 |  |
| (ii) | $\frac{2}{8} \times \frac{3}{7}+\frac{3}{8} \times \frac{2}{7} \text { or } 2 \times \frac{2}{8} \times \frac{3}{7} \text { oe }$ |  |  | M1 for one correct product <br> M1 for completely correct expression |  |  |
|  |  | $\frac{12}{56}$ |  | A1 for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21 |  |  |
|  |  |  |  | Note for (b)(ii): sample space method award 3 marks for correct answer; otherwise no marks <br> $S C$ M1 for $\frac{2}{8} \times \frac{3}{8}$ or $\frac{3}{8} \times \frac{2}{8}$ <br> M1 (dep) for $\frac{2}{8} \times \frac{3}{8}+\frac{3}{8} \times \frac{2}{8}$ oe <br> SC Sample space method - award 2 marks for $\frac{12}{64}$ oe; otherwise no marks |  |  |
|  |  |  |  | Total 7 marks |  |  |


| 17. (a) |  | 2 | 1 | B1 | cao |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  | $x<6$ | 2 |  | $\begin{aligned} & \text { cao B1 for eg } x \leq 6 \\ & \text { or } \ldots-2,-1,0,1,2,3,4,5 \\ & S C \text { B1 for } x \geq 6 \\ & \hline \end{aligned}$ |
| (c) |  | 7 | 1 | B1 | cao |
| (d) | $\mathrm{g}(0)=15$ |  | 2 | M1 | for 15 seen |
|  |  | 3 |  | A1 | cao If M0, award B1 for $\pm 3$ oe |
| (e) | $k=12$ |  | 3 | M1 | May be stated or indicated on diagram. May be implied by one correct solution. |
|  |  | -0.7 or -0.83 .8 |  | A2 | A1 for solution rounding to -0.7 or -0.8 <br> A1 for solution rounding to 3.8 |
| (f) | tan drawn at $x=3.5$ |  | 3 | M1 | tan or tan produced passes between points ( $3,3 \leq y \leq 6$ ) and $(4,11 \leq y \leq 14)$ |
|  | vertical difference horizontal difference |  |  |  | finds their $\frac{\text { vertical difference }}{\text { horizontal difference }}$ for two points on tan or finds their vertical difference horizontal difference for two points on curve, where one of the points has an $x$-coordinate between 3 and 3.5 inc and the other point has an $x$-coordinate between 3.5 and 4 inc |
|  |  | $6.5-11 \mathrm{inc}$ |  | A1 | dep on both M marks |
|  |  |  |  |  | Total 12 marks |


| 18. | $\left(\cos x^{\circ}=\right) \frac{4^{2}+6^{2}-8^{2}}{2 \times 4 \times 6}$ <br> or $8^{2}=4^{2}+6^{2}-2 \times 4 \times 6 \cos x^{\circ}$ | 3 | M1for correct substitution in Cosine <br> Rule$\left(\begin{array}{ll}\left(\cos x^{\circ}=\right)-0.25 \text { oe } & 104.5 \\ \hline & \end{array} \quad \begin{array}{ll}\text { A1 } \begin{array}{l}\text { for value rounding to } 104.5 \\ (104.4775 \ldots)\end{array} \\ \hline & \\ \hline\end{array} \quad\right.$ Total 3 marks |
| :--- | :--- | :--- | :--- | :--- |


| 19. (a) |  |  | 2 | B2 for all correct <br>  B1 for 2 or 3 correct |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b)(i) |  | 10 | 2 | B1 | cao |
| (ii) |  | 25 |  | B1 | cao |
|  |  |  |  |  | Total 4 marks |


| 20. | $\pi \times r \times 9=100$ oe |  | 5 | M1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ( $r=$ ) 3.53677... |  |  |  | for 3.53 or for value rounding to 3.54 (3.14 $\rightarrow 3.53857 \ldots$ ) |
|  | $\sqrt{9^{2}-" 3.53 \ldots{ }^{2}}$ |  |  | M1 |  |
|  | ( $h=$ ) 8.2759... |  |  |  | for 8.27 or for value rounding to 8.28 |
|  |  | 108 |  |  | for answer rounding to 108 $(\pi \rightarrow 108.40 \ldots$ <br> $3.14 \rightarrow 108.45 \ldots$ ) <br> If both M1s scored , award 5 marks for an answer which rounds to 108 |
|  |  |  |  |  | Total 5 marks |


| 21. (a) |  | $8 y^{6}$ | 2 | B 2 | B 1 for 8 B1 for $y^{6}$ |
| :--- | :--- | ---: | ---: | ---: | ---: |
|  | (b) | $2^{p} \times\left(2^{3}\right)^{q}=2^{p} \times 2^{3 q}=2^{p+3 q}$ | $p+3 q$ | 2 | $\mathrm{~B} 2 \quad \mathrm{~B} 1$ for $2^{3 q}$ seen |
|  |  |  |  |  |  |
| Total 4 marks |  |  |  |  |  |


| 22. (a)(i) |  | $3 \mathbf{a}+3 \mathbf{b}$ oe | 3 | B1 ${ }^{\text {B1 }}$ Accept eg $\frac{2}{3}(3 \mathbf{a}+3 \mathbf{b})$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (ii) |  | $2 \mathbf{a}+2 \mathbf{b}$ oe |  |  |  |
| (iii) |  | $\mathbf{a}+2 \mathbf{b}$ oe |  | B1 | Accept eg $2 \mathbf{a}+2 \mathbf{b}-\mathbf{a}$ |
| (b) | $\overrightarrow{D F}=2 \mathbf{a}+4 \mathbf{b} \text { oe }$ |  | 2 | M1 | Also award for $\overrightarrow{E F}=\mathbf{a}+2 \mathbf{b}$ oe |
|  |  | $\begin{aligned} & \overrightarrow{D F}=2 \overrightarrow{D E} \text { oe } \\ & \quad \operatorname{eg} \overrightarrow{D E}=\overrightarrow{E F} \end{aligned}$ |  | A1 | Also award A1 for an acceptable explanation in words. |
|  |  |  |  |  | Total 5 marks |

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Email publication.orders@edexcel.com
Order Code UG030750 January 2012


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