

Mark Scheme (Results)

January 2012

International GCSE Mathematics (4MA0) Paper 4H

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Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answ er	Mark	Notes
1.	$\frac{4.2}{1.12}$		2	M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$
		3.75		A1
				Total 2 marks

2.	135		3	M1
	$\overline{180}$			
	0.75 oe			A1
		45		A1 cao
				Total 3 marks

3.	4x = 7 or 4x = 2 + 5		3	M2	for correct rearrangement with x
	or $7x - 3x = 7$ oe				terms on one side and numbers on
	or $4x - 7 = 0$ oe				the other AND collection of terms
					on at least one side
					or for $4x - 7 = 0$ oe
					M1 for $7x - 3x = 2 + 5$ oe
					ie correct rearrangement with x
					terms on one side and numbers on
					the other
		$1\frac{3}{1}$ oe		A1	Award full marks for a correct
		4		AI	answer if at least 1 method mark
					scored
					Total 3 marks
4.	1 7 7		3	B2	for 1 7 7 in any order
					B1 for three positive whole
					numbers with either a median of 7
					or a sum of 15
					SC Award B1 for 0 7 8
		6		B1	cao
					Total 3 marks
	•			•	
5.	One correct point plotted or stated		4	B1	May appear in table
	2nd correct point plotted or stated			B1	May appear in table
	Correct line betw	yeen x = -2 and x = 4		B2	B1 for a line joining two correct,
					plotted points
					Total 4 marks

6.	(a)	1 + 7 or 8		2	M1		tor of r coefficient ation such as	SC If M0 A0, award B1 for 4:28
			28		A1	cao		
	(b)	32 × 45 or 1440 or 14.4(0)m		3	M1			
		" <u>1440"</u> 72			M1	dep		
			20		A1	cao		
							To	tal 5 marks
					•			
7.		Fully correct factor tree or repeated division or 2, 2, 2, 5, 5 or $2 \times 2 \times 2 \times 5 \times 5$		3	M2		ctor tree or re with 2 and 5 as	
			$2^{3} \times 5^{2}$		A1	Also acce	ept 2 ³ .5 ²	
							To	tal 3 marks
l .					ı			
8.		$y^{3+n-1} = y^6_{\text{ oe or }} y^{3+n} = y^7_{\text{ oe}}$ or $3+n-1=6$ oe or $y^n = \frac{y^7}{y^3}$ or $y^n = \frac{y^6}{y^2}$ or $y^n = y^4$		2	M1		SC if M0, aw an answer of	
			4		A1	cao		
							To	tal 2 marks

9.	(a)	Complete, correct expression which, if correctly evaluated, gives 48 eg		3	M2	M1 for correct expression for area of one relevant triangle
		$4 \times \frac{1}{2} \times 6 \times 4$, $2 \times \frac{1}{2} \times 12 \times 4$, $\frac{1}{2} \times 12 \times 8$				eg $\frac{1}{2} \times 6 \times 4$, $\frac{1}{2} \times 6 \times 4 \sin 90^{\circ}$,
						$\frac{1}{2} \times 8 \times 6, \frac{1}{2} \times 12 \times 4$
			48		A1	cao
	(b)	$4^2 + 6^2 = 16 + 36 = 52$		3	M1	for squaring and adding
		$\sqrt{4^2+6^2}$			M1	(dep) for square root
			7.21		A1	for answer which rounds to 7.21 (7.211102)
						Total 6 marks
10.	(i)		$-1\frac{1}{2} < x \le 2$	4	B2	Also accept $-\frac{3}{2} < x \le 2$ or answer
10.	(i)		$-1\frac{1}{2} < x \le 2$	4	B2	Also accept $-\frac{3}{2} < x \le 2$ or answer expressed as two separate inequalities
10.	(i)		$-1\frac{1}{2} < x \le 2$	4	B2	expressed as two separate
10.	(i)		$-1\frac{1}{2} < x \le 2$	4	B2	expressed as two separate inequalities B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$ or $x \le 2$ (these may be as part of a
10.	(i)		$-1\frac{1}{2} < x \le 2$	4	B2	expressed as two separate inequalities B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$ or $x \le 2$ (these may be as part of a double-ended inequality)
10.			$-1\frac{1}{2} < x \le 2$	4	B2	expressed as two separate inequalities B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$ or $x \le 2$ (these may be as part of a double-ended inequality) or $-\frac{6}{4} < x \le \frac{8}{4}$
10.	(i)		$-1\frac{1}{2} < x \le 2$ $-1 0 1 2$	4	B2	expressed as two separate inequalities B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$ or $x \le 2$ (these may be as part of a double-ended inequality)

Total 4 marks

11. (a)	$75 = 3 \times 5^2$ and $90 = 2 \times 3^2 \times 5$ or 1,3,5,15,25,75 and 1,2,3,5,6,9,10,15,18,30,45,90 or 3×5	2	M1	Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 Prime factors may be shown as factor trees or repeated division
		15	A1	-
(b)	$2 \times 3^2 \times 5^2$ oe eg $6 \times 3 \times 5^2$ or $75,150,225,300,375,450$ and $90,180,270,360,450$	2	M1	Also award for $\frac{75 \times 90}{15}$
		450	A1	
				Total 4 marks

12. (a)	Rotation	3	B1			
	90°		B1	Also accept quarter turn or -270° (B0 for 90° clockwise)	indepe award the ans a singl	
	(0,0)		B1	Also accept origin, O	transfo	ormation
(b)	R correct	1	B1			
(c)	Rotation 90°	2	B1	Accept quarter t -270° instead of		As for (a)
	(3, 1)		B1	ft from their R i a translation of to		
					Tot	al 6 marks

13. (a)	4y = 10 - 3x or $-4y = 3x - 10$		3	M1	May be implied by second M1 or
					by $y = -\frac{3}{4}x + c$ even if value of c
					is incorrect.
					or finds coordinates of 2 points on
					the line eg $(0, 2.5)$, $x = 2$, $y = 1$, table, diagram.
	5 3 10 3			M1	or for clear attempt to evaluate
	$y = \frac{5}{2} - \frac{3}{4}x$ oe or $y = \frac{10}{4} - \frac{3}{4}x$ oe				vert diff horiz diff for their pts
	or $y = \frac{10 - 3x}{100}$ oe				horiz diff
	or $y = \frac{1}{4}$ oc				
		$-\frac{3}{2}$		A1	Award 3 marks for correct answer
		4		711	if either first M1scored or no working shown.
					SC If M0, award B1 for $-\frac{3}{4}x$

13	(b)	eg $9x + 12y = 30$	eg $15x + 20y = 50$		5	M1	for coefficients of x or y the same
		10x - 12y = 46	15x - 18y = 69				or for correct rearrangement of
							one equation followed by correct
							substitution in the other
							eg $5x - 6\left(\frac{10 - 3x}{4}\right) = 23$
		4	v = -1			. 1	1 1/1
		x = 4	$y=-\frac{1}{2}$			A1	cao dep on M1
						M1	(dep on 1st M1) for substituting
							for other variable
				$x = 4$, $y = -\frac{1}{4}$		A1	Award 4 marks for correct values
				$x-4, y-\frac{1}{2}$		ΛI	if at least first M1 scored
				$(4, -\frac{1}{2})$		B1	Award 5 marks for correct answer
				$(4, -\frac{1}{2})$		DI	if at least first M1 scored
							ft from their values of x and y
							Total 8 marks

14.	(a)	55 11.	5 155 177 190 200	1	B1	cao
	(b)		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table ie
						clear attempt to add frequencies
			Curve		B1	ft from points if 4 or 5 correct
			or			or ft correctly from sensible table
			line segments			or if points are plotted consistently
						within each interval at the correct
						heights
						Accept curve which is not joined
	(a)	26 indicated on of growth		2	M1	to the origin
	(c)	26 indicated on cf graph		2	IVII	for 26 indicated on cf graph – accept 26-27 inc
			approx 60 from		A1	If M1 scored, ft from cf graph
			correct graph		А	If M1 not scored, ft only from
			correct graph			correct curve & if answer is
						correct (± ½ sq tolerance) award
						M1 A1
						Total 5 marks
15.			-4 < x < 4	2	B2	B1 for $x < 4$ or $x > -4$ or $x < \pm 4$
						or $x < \sqrt{16}$
						SC B1 for $-4 \le x \le 4$
						Total 2 marks

16.	(a)	$\frac{3}{8} + \frac{2}{8}$ oe		2	M1
			$\frac{5}{8}$		A1
	(b)(i)	$\frac{2}{8} \times \frac{1}{7}$ appearing once only		5	M1 Sample space method –
			$\frac{2}{56}$ or $\frac{1}{28}$		A1 for $\frac{2}{56}$ or $\frac{1}{28}$ or for 0.036 or for answer rounding to 0.036 award 2 marks for correct answer; otherwise no marks
	(ii)	$\frac{2}{8} \times \frac{3}{7} + \frac{3}{8} \times \frac{2}{7} \text{ or } 2 \times \frac{2}{8} \times \frac{3}{7} \text{ oe}$			M1 for one correct product M1 for completely correct expression
			$\frac{12}{56}$		A1 for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21
					Note for (b)(ii): sample space method – award 3 marks for correct answer; otherwise no marks SC M1 for $\frac{2}{8} \times \frac{3}{8}$ or $\frac{3}{8} \times \frac{2}{8}$ M1 (dep) for $\frac{2}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{2}{8}$ oe SC Sample space method – award 2 marks for $\frac{12}{64}$ oe; otherwise no marks
					Total 7 marks

(b) $x < 6 2 B2 cao B1 \text{ for } eg \ x \le 6 \\ or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ SC B1 \text{ for } x \ge 6 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ Or \dots -2, -1, 0, 1, 2, 3, 4, 5 \\ Or \dots -2, -1, 0, 1, 2, 3, 4 \\ Or \dots -2, -1$	17.	(a)		2	1	B1 cao
(c) 7 1 B1 Cao (d) g(0) = 15 2 M1 for 15 seen (e) $k = 12$ 3 M1 May be stated or indicated on diagram. May be implied by one correct solution.		(b)		<i>x</i> < 6	2	B2 cao B1 for eg $x \le 6$
(c) 7 1 B1 cao (d) $g(0) = 15$ 2 M1 for 15 seen (e) $k = 12$ 3 M1 May be stated or indicated on diagram. May be implied by one correct solution. (e) $k = 12$ 3 M1 May be stated or indicated on diagram. May be implied by one correct solution. (f) tan drawn at $x = 3.5$ A2 A1 for solution rounding to -0.7 or -0.8 A1 for solution rounding to 3.8 and $(4, 11 \le y \le 14)$ (f) tan drawn at $x = 3.5$ 3 M1 tan or tan produced passes between points $(3, 3 \le y \le 6)$ and $(4, 11 \le y \le 14)$ Vertical difference horizontal difference for two points on tan or finds their vertical difference for two points on tan or finds their vertical difference for two points on curve, where one of the points has an x -coordinate between 3.5 and 4 inc M1 M2 M3 M4						or2, -1, 0, 1, 2, 3, 4, 5
(d) $g(0) = 15$ 2 M1 for 15 seen A1 cao If M0, award B1 for ± 3 oe (e) $k = 12$ 3 M1 May be stated or indicated on diagram. May be implied by one correct solution. -0.7 or -0.8 3.8 (f) tan drawn at $x = 3.5$ 3 M1 tan or tan produced passes between points $(3, 3 \le y \le 6)$ and $(4, 11 \le y \le 14)$ vertical difference horizontal difference for two points on tan or finds their vertical difference for two points on curve, where one of the point has an x -coordinate between 3 and 3.5 inc and the other point has an x -coordinate between 3.5 and 4 inc (6.5 - 11 inc) A1 dep on both M marks						$SC B1 $ for $x \ge 6$
(e) $k=12$ 3		(c)		7	1	
(e) $k=12$ 3 M1 May be stated or indicated on diagram. May be implied by one correct solution. -0.7 or -0.8 3.8 (f) tan drawn at $x=3.5$ 2 A1 for solution rounding to -0.7 or -0.8 A1 for solution rounding to 3.8 tan or tan produced passes between points $(3, 3 \le y \le 6)$ and $(4, 11 \le y \le 14)$ Vertical difference horizontal difference for two points on tan or finds their vertical difference for two points on tan or finds their vertical difference for two points on curve, where one of the point has an x -coordinate between 3 and 3.5 inc and the other point has an x -coordinate between 3.5 and 4 inc 6.5 - 11 inc A1 dep on both M marks		(d)	g(0) = 15		2	M1 for 15 seen
diagram. May be implied by one correct solution.				3		A1 cao If M0, award B1 for ± 3 oe
(f) $tan drawn at x = 3.5$ (f) $tan drawn at x = 3.5$ (g) $tan drawn at x = 3.5$ (h) $tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (h) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (h) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (h) tan or tan produced passes between points on tan or finds their vertical difference for two points on tan or finds their vertical difference for two points on curve, where one of the points has an x-coordinate between 3 and 3.5 inc and the other point has an x-coordinate between 3.5 and 4 inc (a) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (b) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (b) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (b) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (c) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (d) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (e) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (f) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (f) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (f) tan or tan produced passes between points (4, 11 \le y \le 14) (f) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (g) tan or tan produced passes between points (3, 3 \le y \le 6) and (4, 11 \le y \le 14) (g) tan or tan produced passes between points (4, 11 \le y \le 14) (g) tan or tan produced passes between points (4, 11 \le y \le 14) (g) tan or tan produced passes between points (4, 11 \le y \le 14) (g) tan or tan produced passes between points (4, 11 \le y \le 14) (g) tan o$		(e)	k = 12		3	diagram. May be implied by one
between points $(3, 3 \le y \le 6)$ and $(4, 11 \le y \le 14)$ Purical difference horizontal difference horizontal difference horizontal difference for two points on tan or finds their vertical difference horizontal difference horizontal difference horizontal difference for two points on curve, where one of the points has an x-coordinate between 3 and 3.5 inc and the other point has an x-coordinate between 3.5 and 4 inc 6.5 – 11 inc A1 dep on both M marks				-0.7 or -0.8 3.8		−0.7 or −0.8
horizontal difference finds their horizontal difference for two points on tan or finds their vertical difference horizontal difference horizontal difference for two points on curve, where one of the points has an x-coordinate between 3 and 3.5 inc and the other point has an x-coordinate between 3.5 and 4 inc 6.5 – 11 inc A1 dep on both M marks		(f)	tan drawn at $x = 3.5$		3	between points $(3, 3 \le y \le 6)$ and
Total 12 marks				6.5 – 11 inc		finds their horizontal difference for two points on tan or finds their vertical difference horizontal difference for two points on curve, where one of the points has an x-coordinate between 3 and 3.5 inc and the other point has an x-coordinate between 3.5 and 4 inc
						1

18.	$(\cos x^{\circ}) = \frac{4^{2} + 6^{2} - 8^{2}}{2 \times 4 \times 6}$ or $8^{2} = 4^{2} + 6^{2} - 2 \times 4 \times 6 \cos x^{\circ}$		3	M1 for correct substitution in Cosine Rule
	$(\cos x^{\circ} =) -0.25 \text{ oe}$			A1
		104.5		A1 for value rounding to 104.5 (104.4775)
				Total 3 marks

19. (a)	7	10 (12) 8 B	2	B2	for all correct B1 for 2 or 3 correct
(b)(i)		10	2	B1	cao
(ii)		25		B1	cao
					Total 4 marks

20.		$\pi \times r \times 9 = 100$ oe		5	M1	
		(<i>r</i> =) 3.53677			A1	for 3.53
						or for value rounding to 3.54
						$(3.14 \rightarrow 3.53857)$
		$\sqrt{9^2 - "3.53"^2}$			M1	
		(h =) 8.2759			A1	for 8.27
						or for value rounding to 8.28
			108		A1	for answer rounding to 108
						$(\pi \rightarrow 108.40$
						$3.14 \rightarrow 108.45)$
						If both M1s scored, award 5 marks for an answer which rounds
						to 108
						Total 5 marks
				Ī	_	
21.	(a)		$8y^6$	2	B2	B1 for 8 B1 for y^6
	(b)	$2^p \times (2^3)^q = 2^p \times 2^{3q} = 2^{p+3q}$	p+3q	2	B2	B1 for 2^{3q} seen
						Total 4 marks
					•	
22.	(a)(i)		3 a + 3 b oe	3	B1	
	(ii)		$2\mathbf{a} + 2\mathbf{b}$ oe		B1	Accept eg $\frac{2}{3}(3\mathbf{a} + 3\mathbf{b})$
	(iii)		a + 2 b oe		B1	Accept eg $2\mathbf{a} + 2\mathbf{b} - \mathbf{a}$
	(b)	$\frac{\Rightarrow}{DF} = 2\mathbf{a} + 4\mathbf{b} \text{ oe}$		2	M1	Also award for $\overrightarrow{EF} = \mathbf{a} + 2\mathbf{b}$ oe
			$ \begin{array}{c} $		A1	Also award A1 for an acceptable explanation in words.
						Total 5 marks

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